

39. $f(x) = \begin{cases} 3-x, & x < 1 \quad \text{left} \\ ax^2 + bx, & x \geq 1 \quad \text{right} \end{cases}$

a) continuous

$$\lim_{x \rightarrow 1^-} 3-x = 2$$

$$\lim_{x \rightarrow 1^+} ax^2 + bx = a+b$$

$$\boxed{a+b = 2}$$

b) differentiable

left -1

right $2ax + b \big|_{x=1} = 2a+b$

$$\boxed{2a+b = -1}$$

$$a+b = 2$$

$$2a+b = -1$$

$$\hline -a = 3$$

$$a = -3$$

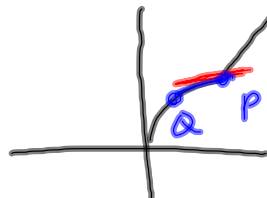
$$b = 5$$

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23 $y = x^{2/3}$ $x = 0$

numerical der.

3 $y = \begin{cases} \sqrt{x}, & x < 1 \\ 2x-1, & x \geq 1 \end{cases}$



left

$$x_1 = 1$$

$$y_1 = 1$$

$$x_2 = b$$

$$y_2 = \sqrt{b}$$

$$\lim_{b \rightarrow 1} \frac{(\sqrt{b}-1)(\sqrt{b}+1)}{(b-1)(\sqrt{b}+1)}$$

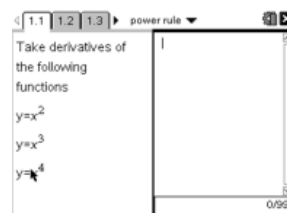
$$\lim_{b \rightarrow 1} \frac{\cancel{b-1}}{(\cancel{b-1})(\sqrt{b}+1)} = \frac{1}{2}$$

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3.3a Rules for Differentiation

Use Power Rule.tns to discover the power rule for derivatives

$$\frac{d}{dx} x^n = n x^{n-1}$$



$$\frac{d}{dx} x^2 = 2x$$

$$\frac{d}{dx} x^3 = 3x^2$$

$$\frac{d}{dx} x^5 = 5x^4$$

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$$\frac{d}{dx} ax^n = a \cdot n x^{n-1}$$

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Proof of the power rule

$$y = x^n \quad \text{prove} \quad \frac{dy}{dx} = nx^{n-1}$$

$$x_1 = x \quad \lim_{h \rightarrow 0} \frac{(x+h)^n - x^n}{h}$$

$$y_1 = x^n$$

$$x_2 = x+h \quad \lim_{h \rightarrow 0} \frac{\cancel{x^n} + n\cancel{x^{n-1}}h + \cancel{x^{n-2}h^2} \dots \cancel{h^n} - x^n}{h}$$

$$y_2 = (x+h)^n \quad \lim_{h \rightarrow 0} \frac{h(n\cancel{x^{n-1}} + \cancel{x^{n-2}h} \dots)}{h}$$

$n=2$
 $n=3$
 $n=4$

$1 \quad 2 \quad 1$
 $1 \quad 3 \quad 3 \quad 1$
 $1 \quad 4 \quad 6 \quad 4 \quad 1$
 \vdots

nX^{n-1}

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Find $\frac{dy}{dx}$ if $y = x^3 + 6x^2 - \frac{5}{3}x + 16$

$$\frac{dy}{dx} = 3x^2 + 12x - \frac{5}{3}$$

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Find the horizontal tangents of $y = x^4 - 2x^2 + 2$

by hand

$$\frac{dy}{dx} = 4x^3 - 4x$$

we want the
slope = 0
derivative = 0

solve
for x

$$4x^3 - 4x = 0$$

$$4x(x^2 - 1) = 0$$

with the calculator

$$4x(x+1)(x-1) = 0$$

$x=0$	$y=2$
$x=1$	$y=1$
$x=-1$	$y=1$

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higher order derivatives

$$y = 6x^3 + x^2$$

$$y' = \frac{dy}{dx} = 18x^2 + 2x$$

$$y'' = \frac{d^2y}{dx^2} = 36x + 2$$

$$y''' = \frac{d^3y}{dx^3} = 36$$

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